

# Structure from Motion

## summary

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**Version 3.0**

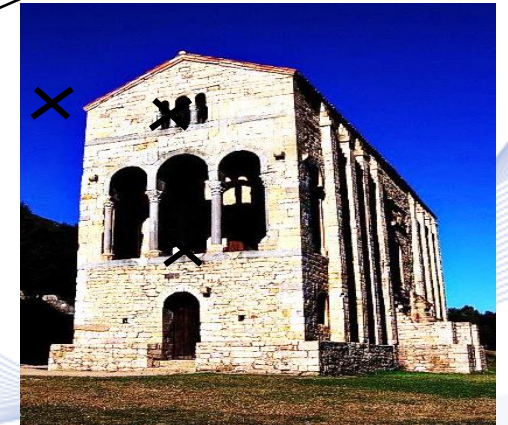
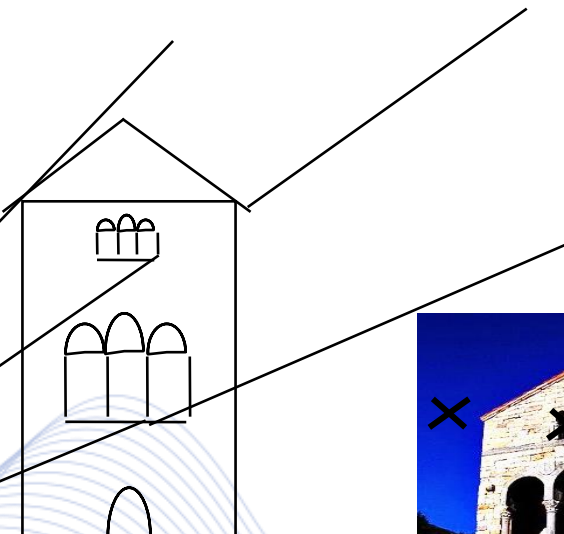
# Structure from Motion

- **Image-based 3D Shape Reconstruction**
- Structure from motion
- Structure from motion applications
- 3D Shape reconstruction workflow issues

# Calibrated monocular image



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# Stereo imaging

- Two cameras in known locations.
- Calibrated cameras.
- Stereo images can create a disparity (depth) map.

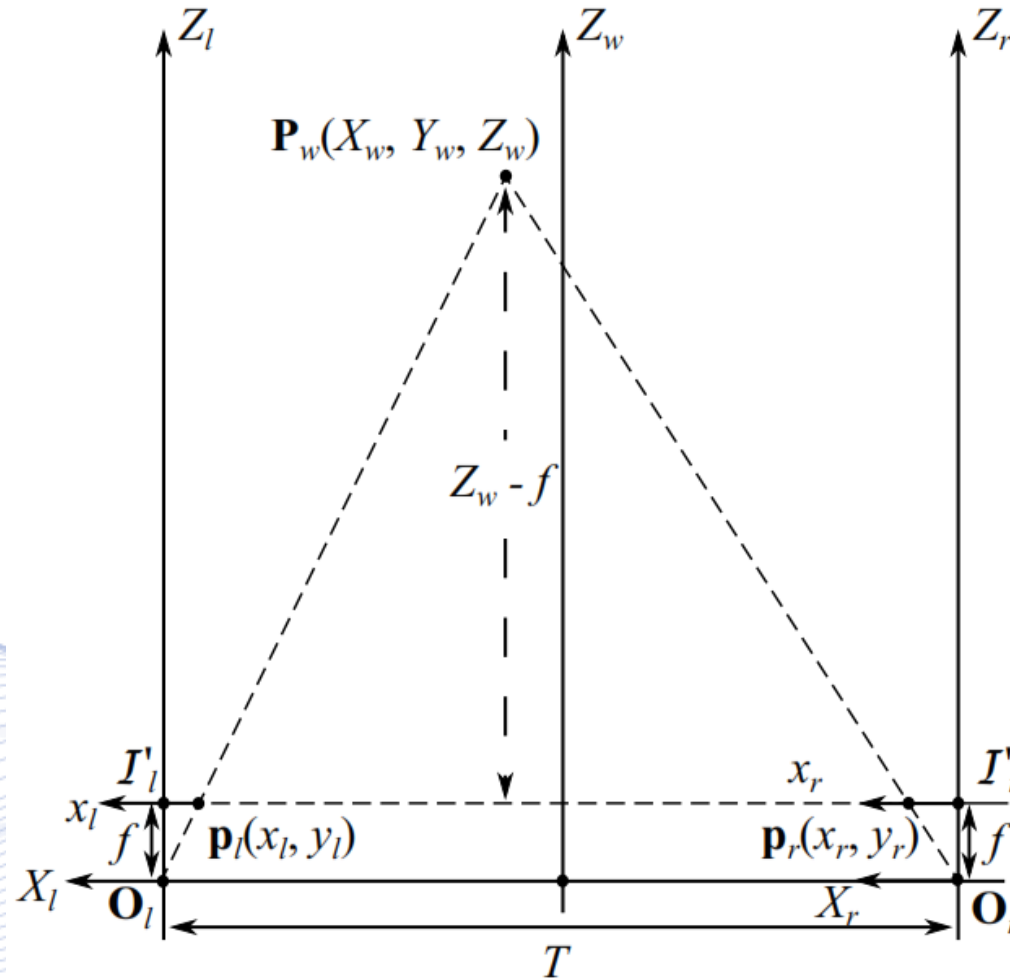


a) Left image; b) Right image; c) Dense disparity map.

# Parallel Camera Setup

## Parallel Stereo vision Geometry

$T$ : baseline  
 $f$ : focal length



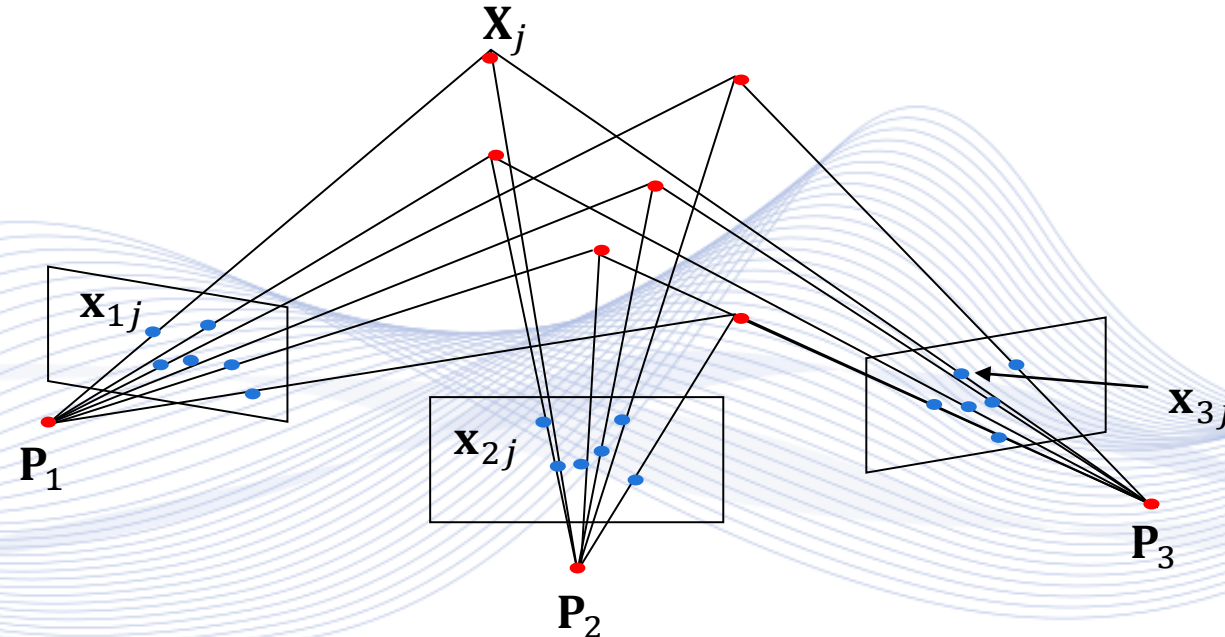
# Feature extraction and matching

- Extract keypoints based on local features.
- Common feature extractors are SIFT, SURF, ORB etc.
- The keypoints are matched between images taken from different views.

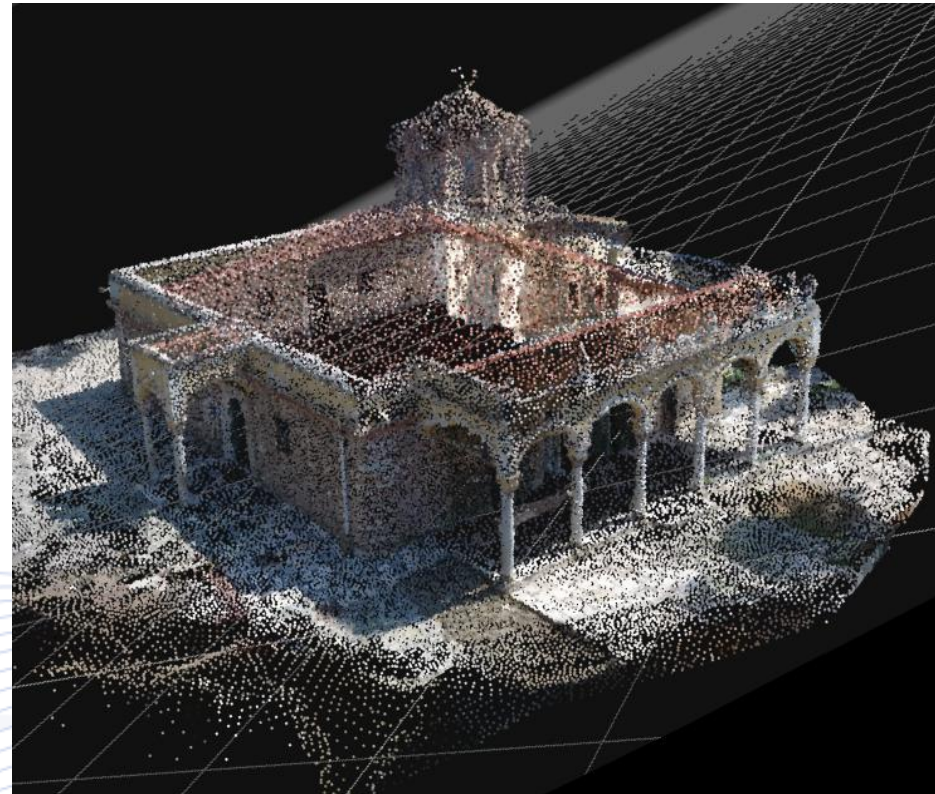


# Triangulation and Bundle Adjustment

- Bundle adjustment and triangulation are the final steps to estimate the camera parameters and create an accurate point cloud.
- Further techniques are used to make the point cloud denser and to reconstruct surface based on it.



# Triangulation and Bundle Adjustment



3D model of Vlatadon monastery.



# Structure from Motion

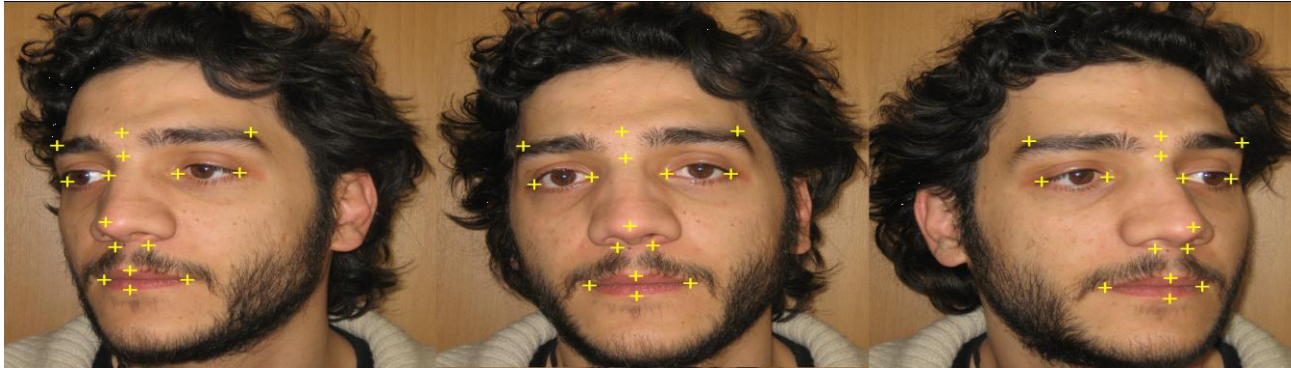
## ***Bundle Adjustment:***

- Initial SfM stages end up providing an accurate initial guess to non-linear re-projection error optimization:

$$\operatorname{argmin}_{\mathbf{P}_i, \mathbf{P}_j} \sum_{i,j} v_{ij} \|\mathbf{p}_{ij} - \mathbf{P}_i \mathbf{P}_j\|^2.$$

- $\mathbf{P}_i$ : projection matrix of camera  $i$ .
- $\mathbf{P}_j$ : world coordinate point  $\mathbf{X}_j$  (homogeneous coordinates).
- $\mathbf{p}_{ij}$ : projection  $\mathbf{x}_{ij}$  on camera  $i$  plane (homogeneous coordinates).
- $v_{ij} = \{0,1\}$ : it denotes if point  $j$  is visible on camera  $i$ .

# SfM in 3D Face Reconstruction



Selected features

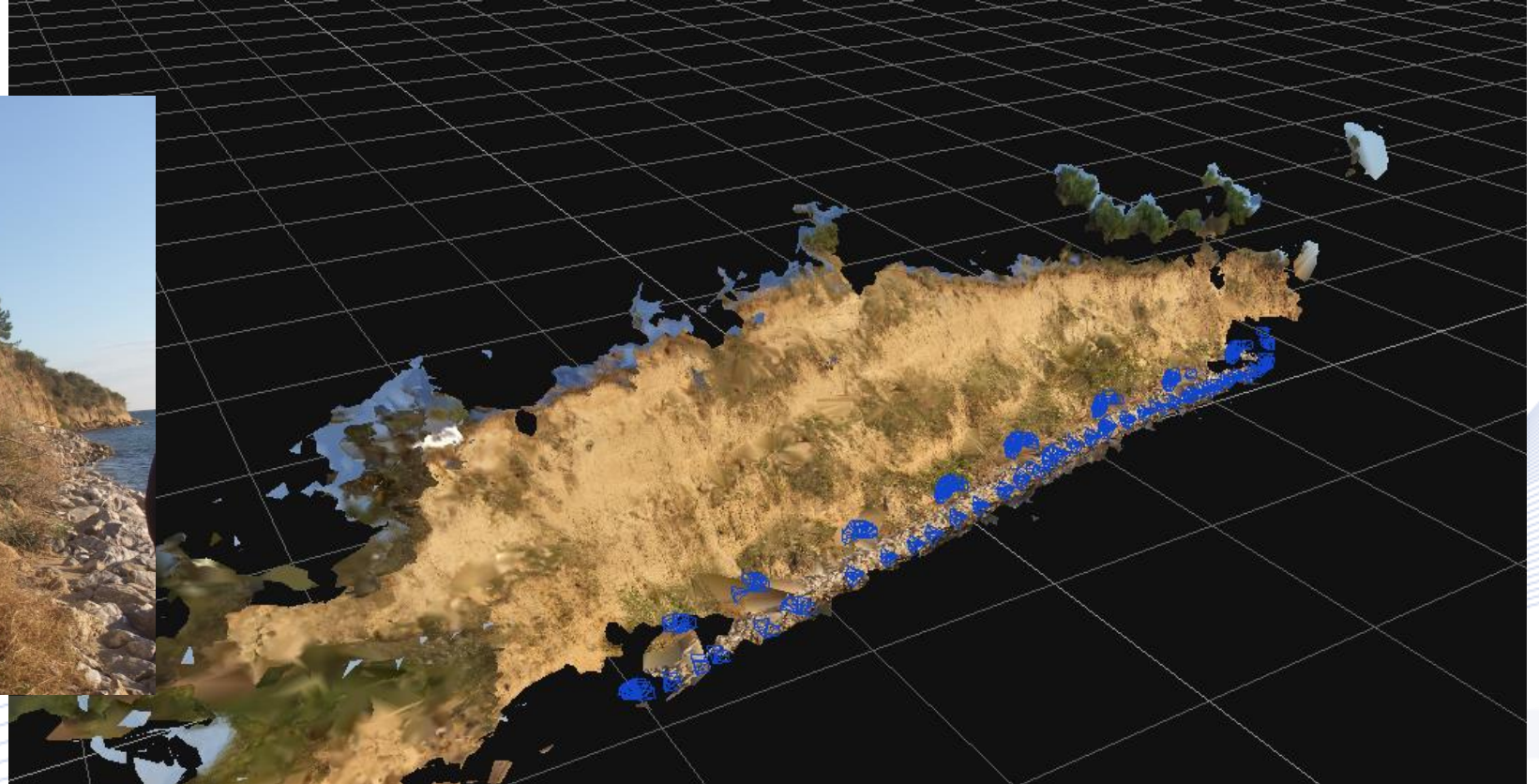


3D face reconstruction



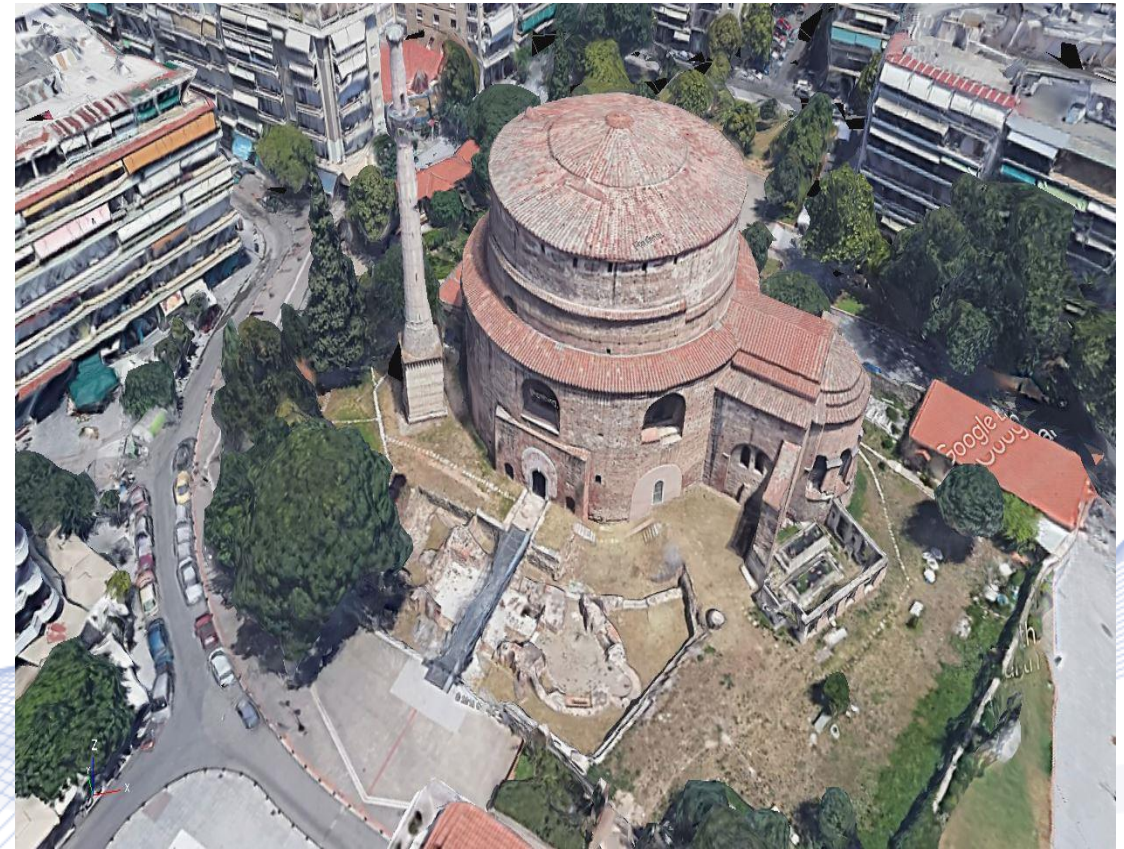
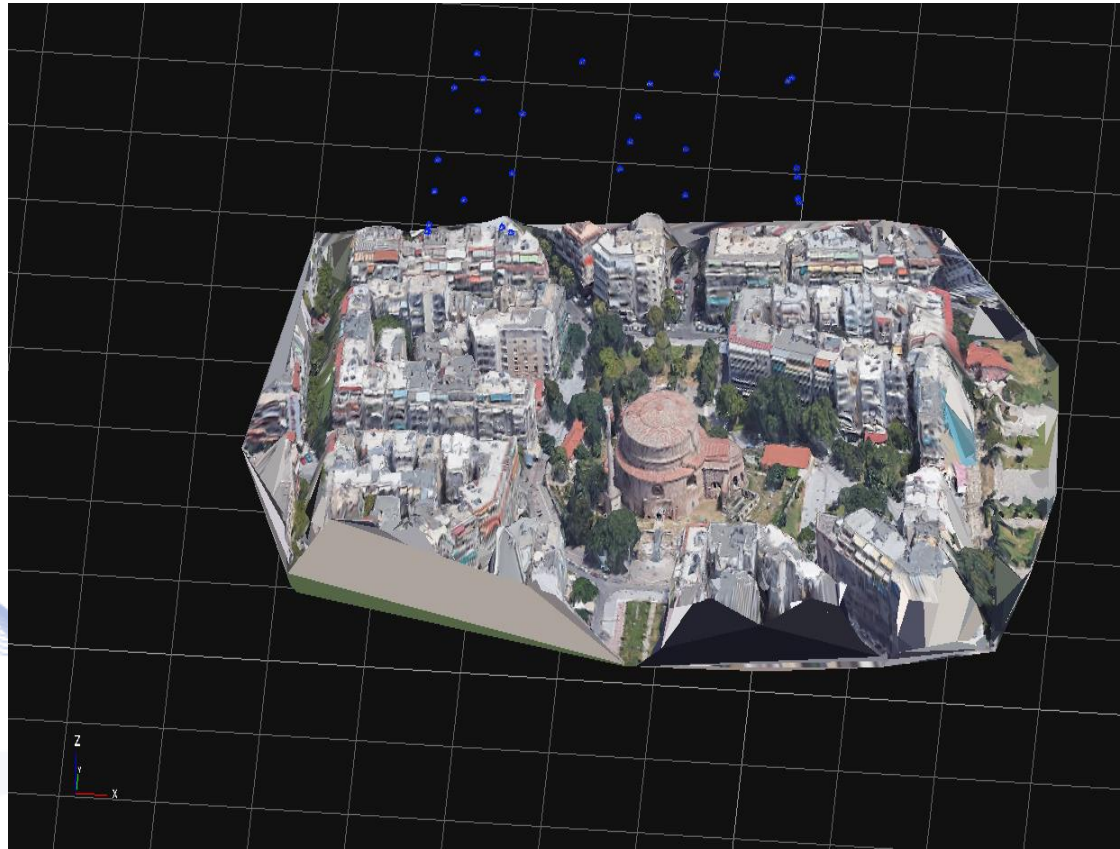
CANDIDE grid reprojection

# SfM in 3D landscape reconstruction



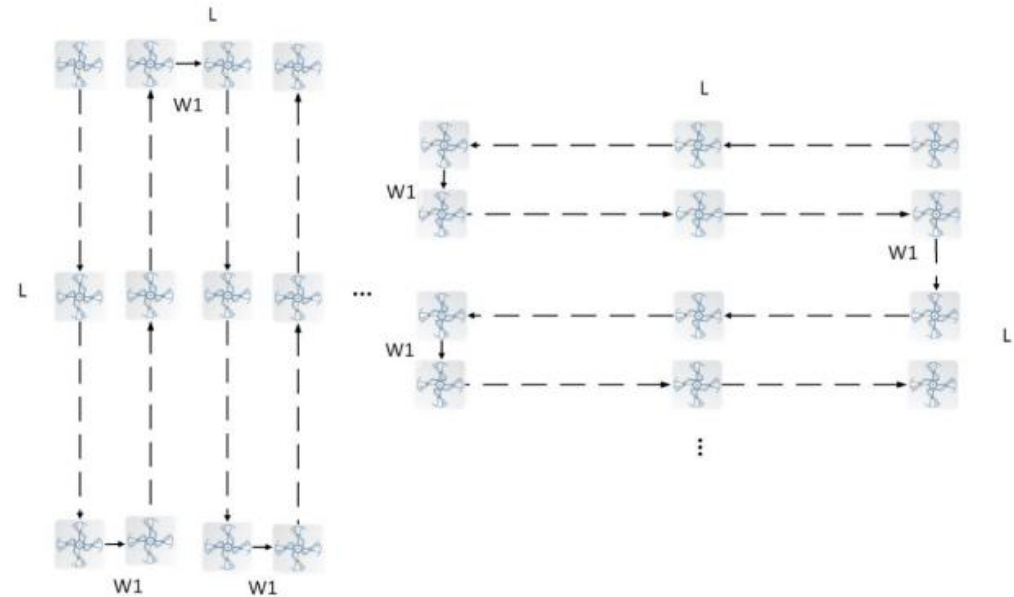
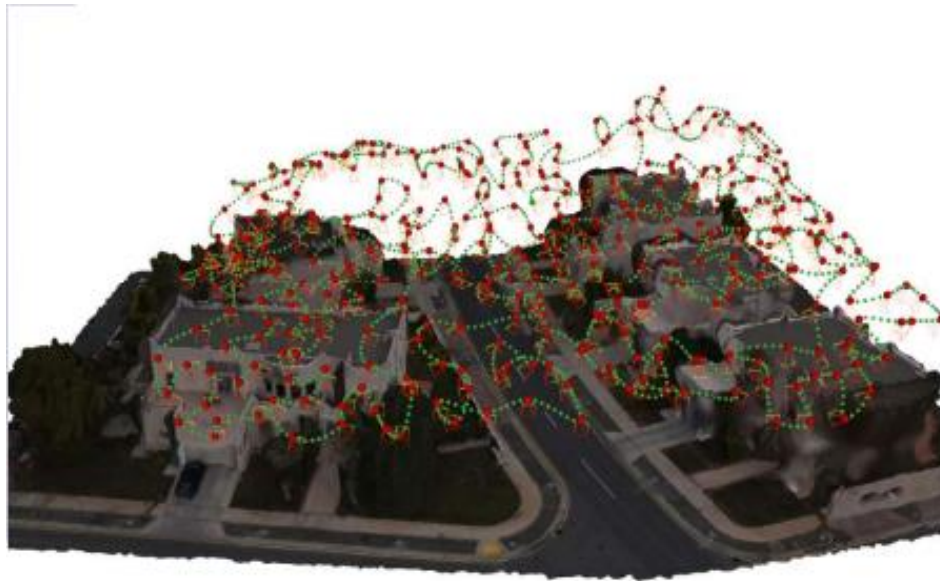
- 3D cliff surface reconstruction

# SfM in 3D monument reconstruction

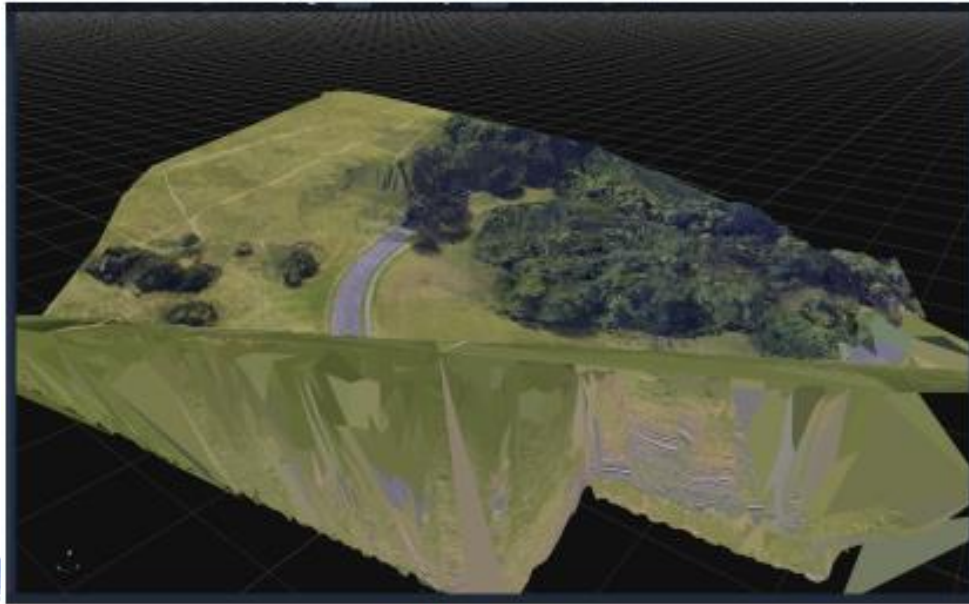


Rotonda monument, Thessaloniki, Greece.

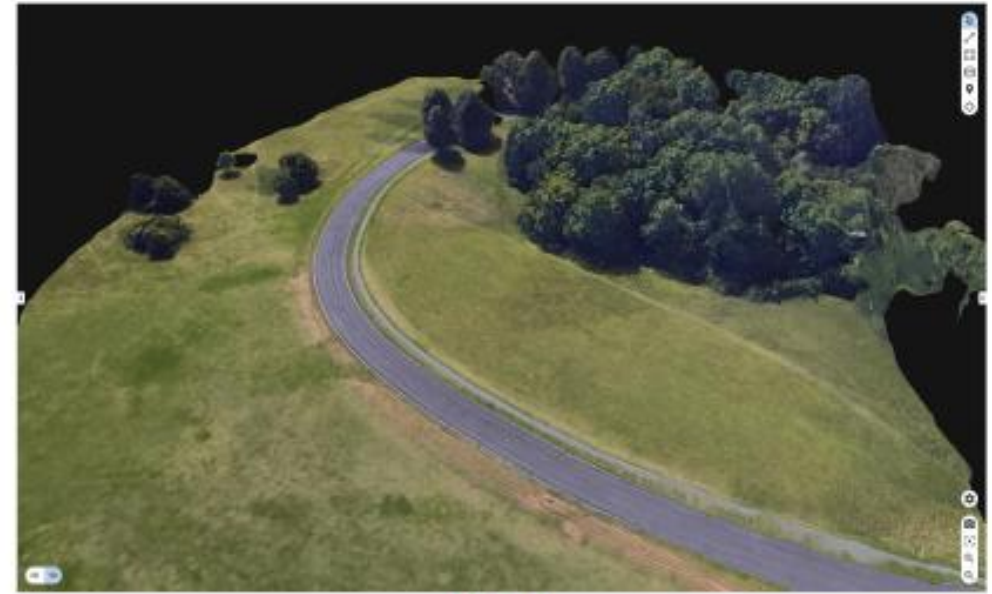
# Optimal UAV Flight Trajectory



# Photogrammetry Reconstruction



3DF Zephyr



Pix4D



# Flat Surface Smoothing

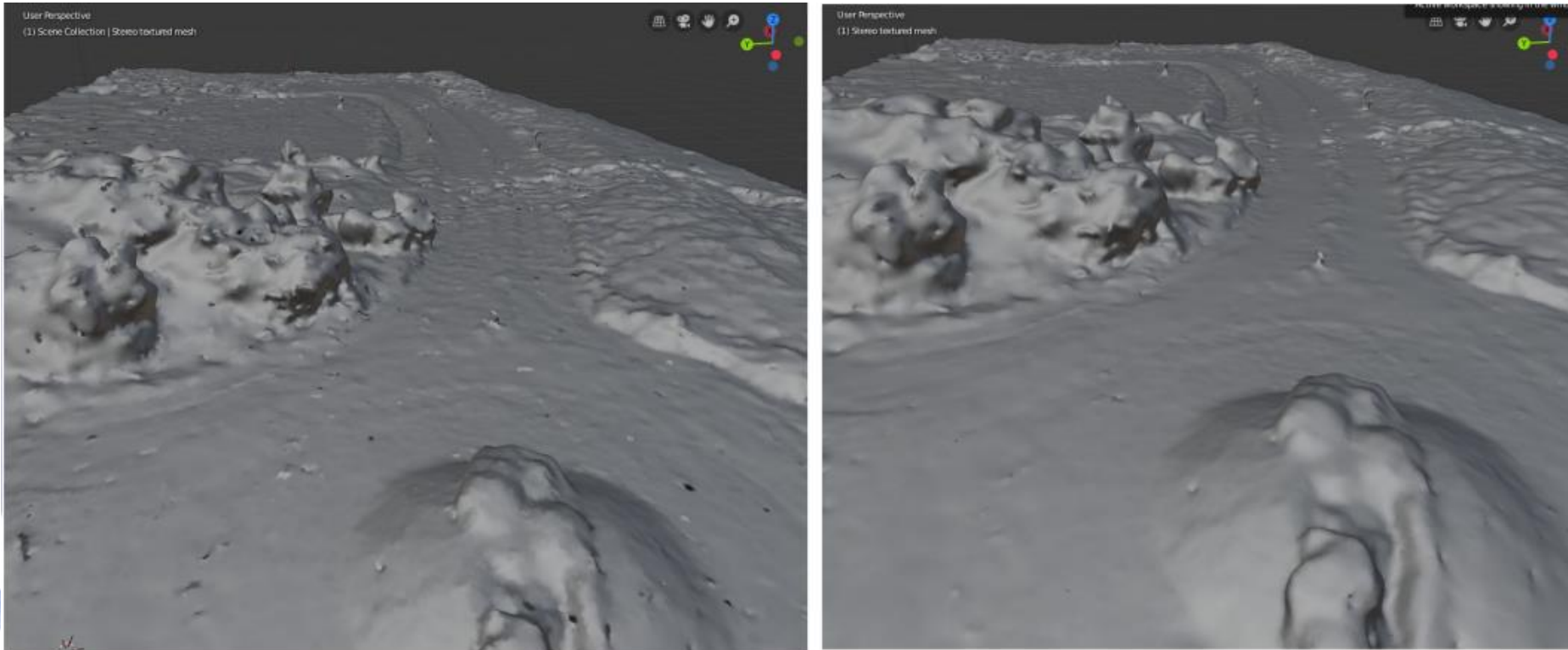


Figure: An example of Smoothing. (Left) The initial 3D model structure. (Right) The processed 3D model structure after Smoothing.

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# Q & A

**Thank you very much for your attention!**

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